

Pythagorean Theorem

$$c^2 = a^2 + b^2$$

Absolute & Relative Error – Accuracy

$$\text{Absolute Error} = |\text{Observed} - \text{Accepted}|$$

$$E_A = |O - A|$$

$$\text{Relative Error} = \frac{\text{Absolute Error}}{\text{Accepted}} \cdot 100\%$$

$$E_R = \frac{E_A}{A} \cdot 100\% = \frac{|O - A|}{A} \cdot 100\%$$

Absolute & Relative Deviation – Precision

$$\text{Absolute Deviation} = |\text{Observed} - \text{Mean}|$$

$$D_A = |O - M|$$

$$\text{Relative Deviation} = \frac{\text{Absolute Deviation}}{\text{Mean}} \cdot 100\%$$

$$D_R = \frac{D_A}{M} \cdot 100\% = \frac{|O - M|}{M} \cdot 100\%$$

Trigonometric Functions

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}} \quad \cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

Resultant

$$\text{Magnitude} = R = \sqrt{R_x^2 + R_y^2} \quad \text{Direction} = \theta = \tan^{-1} \frac{R_y}{R_x}$$

Speed, Velocity & Acceleration

$$\text{Speed}_{av} = \frac{\text{Distance}}{\text{Elapsed Time}} \quad v_{av} = \frac{x_f - x_i}{t_f - t_i} = \frac{\Delta x}{\Delta t}$$

$$a_{av} = \frac{v_f - v_i}{t_f - t_i} = \frac{\Delta v}{\Delta t}$$

Linear Kinematics

$$v_f = v_i + a\Delta t \quad \Delta x = \frac{1}{2}(v_i + v_f)\Delta t$$

$$v_f^2 = v_i^2 + 2a\Delta x \quad \Delta x = v_i t + \frac{1}{2}a\Delta t^2$$

Relative Motion

$$v_{ab} = v_{ac} + v_{cb}$$

Falling Objects & Projectiles

$$v_x = \text{constant}$$

$$g = -9.81 \text{ m/s}^2$$

$$v_{x,i} = v_i(\cos \theta)$$

$$v_{y,i} = v_i(\sin \theta)$$

$$\Delta x = v_i(\cos \theta)\Delta t$$

$$\Delta y = v_{y,i}\Delta t + \frac{1}{2}g\Delta t^2$$

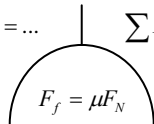
$$v_{y,f} = v_{y,i} + g\Delta t$$

$$v_{y,f}^2 = v_{y,i}^2 + 2g\Delta y$$

Newton's Second Law

$$\sum F = ma \quad \text{@ Equilibrium } \sum F = 0$$

$$\sum F_x = ma_x = \dots \quad \sum F_y = ma_y = \dots$$



Force of Friction

$$F_f = \mu F_N$$

$$F_s = \mu_s F_N \quad F_k = \mu_k F_N$$

Net Work Done by Constant Force

$$W_{net} = F_{net} d(\cos \theta)$$

Kinetic Energy

$$KE = \frac{1}{2}mv^2$$

Potential Energy

$$PE_{gravitational} = U = mgh \quad PE_{elastic} = \frac{1}{2}kx^2$$

Conservation of Mechanical Energy

$$ME_i = ME_f$$

$$KE_i + PE_{g,i} + PE_{e,i} + U_i = KE_f + PE_{g,f} + PE_{e,f} + U_f$$

$$\frac{1}{2}mv_i^2 + mgh_i + \frac{1}{2}kx_i^2 = \frac{1}{2}mv_f^2 + mgh_f + \frac{1}{2}kx_f^2$$

Work-Kinetic Energy Theorem

$$W_{net} = \Delta KE$$

Power

$$P = \frac{\text{Work}}{\text{Time}} = \frac{W}{t} = \frac{Fd}{t} = Fv$$

Momentum

$$p = mv$$

Impulse-Momentum Theorem

$$F\Delta t = \Delta p = mv_f - mv_i$$

Conservation of Momentum

$$mv_{1i} + mv_{2i} = mv_{1f} + mv_{2f}$$

Perfectly Inelastic Collisions

$$m_1v_{1i} + m_2v_{2i} = (m_1 + m_2)v_f$$

$$\frac{1}{2}m_1v_{1i}^2 + \frac{1}{2}m_2v_{2i}^2 \neq \frac{1}{2}(m_1 + m_2)v_f^2$$

or

$$(m_1 + m_2)v_i = mv_{1,f} + mv_{2,f}$$

$$\frac{1}{2}(m_1 + m_2)v_i^2 \neq \frac{1}{2}m_1v_{1,f}^2 + \frac{1}{2}m_2v_{2,f}^2$$

Elastic Collisions

$$m_1v_{1i} + m_2v_{2i} = m_1v_{1f} + m_2v_{2f}$$

$$\frac{1}{2}m_1v_{1i}^2 + \frac{1}{2}m_2v_{2i}^2 = \frac{1}{2}m_1v_{1f}^2 + \frac{1}{2}m_2v_{2f}^2$$

Arc Length

$$\Delta s = r\Delta \theta$$

Angular Velocity

$$\omega_{av} = \frac{\theta_f - \theta_i}{t_f - t_i} = \frac{\Delta \theta}{\Delta t}$$

Angular Acceleration

$$\alpha_{av} = \frac{\omega_f - \omega_i}{t_f - t_i} = \frac{\Delta \omega}{\Delta t}$$

Tangential Speed

$$v_T = r\omega$$

Tangential Acceleration

$$a_T = r\alpha$$

Centripetal Acceleration

$$a_C = \frac{v_T^2}{r} = r\omega^2$$

Centripetal Force

$$F_C = \frac{mv_T^2}{r} = mr\omega^2$$

Newton's Universal Law of Gravitation

$$F = G \frac{m_1 m_2}{r^2} \quad G = 6.6732 \cdot 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2$$

Orbital Period

$$T = 2\pi \sqrt{\frac{r^3}{Gm}}$$

Orbital Speed

$$v_T = \sqrt{\frac{Gm}{r}}$$

Rotational Kinematics

$$\omega_f = \omega_i + \alpha\Delta t \quad \Delta \theta = \frac{1}{2}(\omega_i + \omega_f)\Delta t$$

$$\omega_f^2 = \omega_i^2 + 2\alpha\Delta \theta \quad \Delta \theta = \omega_i t + \frac{1}{2}\alpha\Delta t^2$$

Torque

$$\sum \tau = Fl \quad \text{@ Equilibrium } \sum \tau = 0$$

$$\sum \tau = Fl \cos \theta$$

Heat & Calorimetry

$$Q = mc\Delta T$$

$$Q_{gained} = -Q_{loss}$$

$$m_w c_w \Delta T_w = -m_x c_x \Delta T_x$$

Heat during a Phase Change

$$Q = mL_F \quad Q = mL_V$$

Temperature Conversions

$$K = ^\circ C + 273.15 \quad ^\circ F = \frac{9}{5}(^{\circ}C) + 32$$

$$^{\circ}C = K - 273.15 \quad ^{\circ}C = \frac{5}{9}(^{\circ}F - 32)$$

Work done by a Gas

$$W = P\Delta d = P\Delta V$$

First Law of Thermodynamics

$$\Delta U = Q - W$$

Cyclic Process

$$\Delta U_{net} = 0 \quad Q_{net} = W_{net}$$

Efficiency of a Heat Engine

$$\text{eff} = \frac{W_{net}}{Q_h} = \frac{Q_h - Q_c}{Q_h} = 1 - \frac{Q_c}{Q_h}$$

Elasticity

$$\text{Stress} = \frac{F}{A} \quad \text{Strain} = \frac{\Delta L}{L_0}$$

$$\text{Young's Modulus} = \frac{FL_0}{A\Delta L}$$

Expansion

$$\Delta L = L_0\alpha\Delta T \quad \Delta A = 2A_0\alpha\Delta T$$

$$\Delta V = V_0\beta\Delta T$$

Mass Density

$$\rho = \frac{m}{V}$$

$$\rho_{\text{water}} = 1.0 \cdot 10^3 \text{ kg/m}^3 \quad \rho_{\text{seawater}} = 1.025 \cdot 10^3 \text{ kg/m}^3$$

Buoyant Force on Floating Objects

$$F_B = F_g(\text{Displaced Fluid}) = m_f g$$

$$F_B = F_g(\text{Object}) = m_o g$$

Pressure

$$P_0 = 1.01 \cdot 10^5 \text{ Pa}$$

$$1 \text{ atm} = 101.3 \text{ kPa}$$

$$1.013 \cdot 10^5 \text{ Pa}$$

$$760 \text{ mmHg}$$

$$760 \text{ torr}$$

$$P = \frac{F}{A} = \frac{\text{Force}}{\text{Area}}$$

Fluid Pressure as a Function of Depth

$$P = P_0 + \rho g h$$

Bernoulli's Equation

$$P + \frac{1}{2} \rho v^2 + \rho g h = \text{constant}$$

Gas Laws

$$\text{Combined} \quad \frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\text{Ideal} \quad PV = nRT$$

Hooke's Law

$$F_{\text{elastic}} = -kx$$

Period of a Simple Pendulum - SHM

$$T = 2\pi \sqrt{\frac{L}{g}}$$

Period of a Mass-Spring System- SHM

$$T = 2\pi \sqrt{\frac{m}{k}}$$

Wave Equation

$$v = f\lambda \quad c = f\lambda$$

$$c = 3.00 \cdot 10^8 \text{ m/s}$$

Intensity of a Spherical Wave

$$\text{Intensity} = I = \frac{P}{4\pi r^2}$$

Loudness

$$\beta = (10 \text{ dB}) \log\left(\frac{I}{I_0}\right)$$

$$I_0 = 1 \cdot 10^{-12} \text{ W/m}^2$$

Doppler Effect

$$f_o = f_s \left(\frac{1 \pm \frac{v_o}{v}}{1 \pm \frac{v_s}{v}} \right)$$

Velocity of Wave through a Wire

$$v = \sqrt{\frac{F}{m/L}}$$

Harmonic Series – Vibrating String

$$f_n = n \frac{v}{2L} \quad n = 1, 2, 3, \dots$$

Harmonic Series – Open Pipe

$$f_n = n \frac{v}{2L} \quad n = 1, 2, 3, \dots$$

Harmonic Series – Closed Pipe

$$f_n = n \frac{v}{4L} \quad n = 1, 3, 5, \dots$$

Mirror & Lens Equation

$$\frac{1}{p} + \frac{1}{q} = \frac{2}{r} = \frac{1}{f}$$

Magnification Equation

$$M = \frac{h'}{h} = -\frac{q}{p}$$

Index of Refraction

$$n = \frac{c}{v}$$

Snell's Law

$$n_i(\sin \theta_i) = n_r(\sin \theta_r)$$

Critical Angle

$$\sin \theta_c = \frac{n_r}{n_i} (\sin 90^\circ) = \frac{n_r}{n_i}$$

$$\text{for } n_i > n_r$$

Destructive Interference

$$d(\sin \theta) = (m + \frac{1}{2})\lambda \quad m = 0, \pm 1, \pm 2, \dots$$

Constructive Interference

$$d(\sin \theta) = m\lambda \quad m = 0, \pm 1, \pm 2, \dots$$

Coulomb's Law - Electric Field Strength

$$F_{\text{electric}} = k_c \frac{q_1 q_2}{r^2}$$

Electric Field Strength – Point Charge

$$E = k_c \frac{q}{r^2}$$

Electric Potential Energy – Uniform Field

$$PE_{\text{electric}} = -qEd$$

Potential Difference

$$\Delta V = \frac{\Delta PE_{\text{electric}}}{q} = -E\Delta d$$

Potential Difference - Infinity & Point

$$\Delta V = k_c \frac{q}{r}$$

Capacitance

$$C = \frac{Q}{\Delta V}$$

$$C_{\text{vacuum}} = \epsilon_0 \frac{A}{d}$$

Electrical PE - Stored

$$PE_{\text{electric}} = \frac{1}{2} Q\Delta V = \frac{1}{2} C(\Delta V)^2 = \frac{Q^2}{2C}$$

Electrical Current

$$I = \frac{\Delta Q}{\Delta t} \quad I = \frac{\Delta V}{R_{\text{eq}}}$$

Voltage & Resistance

$$\Delta V = IR \quad R = \frac{\Delta V}{I}$$

Electrical Power

$$P = I\Delta V = I^2 R = \frac{(\Delta V)^2}{R}$$

Series Circuit

$$I_{\text{Total}} = I_1 = I_2 = I_3 = \dots$$

$$emf = \Delta V = V_1 + V_2 + V_3 + \dots$$

$$R_{\text{eq}} = R_1 + R_2 + R_3 + \dots$$

$$\frac{1}{C_{\text{eq}}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots$$

Parallel Circuit

$$I_{\text{Total}} = I_1 + I_2 + I_3 + \dots$$

$$emf = \Delta V = \Delta V_1 = \Delta V_2 = \Delta V_3 = \dots$$

$$\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

$$C_{\text{eq}} = C_1 + C_2 + C_3 + \dots$$

Magnitude of a Magnetic Field

$$B = \frac{F_{\text{magnetic}}}{qv}$$

Force on a Current-Carrying Conductor \perp to a Magnetic Field

$$F_{\text{magnetic}} = B I \ell$$

Energy of Light Quantum

$$E = hf$$

$$\text{Planck's Constant} = 6.63 \cdot 10^{-34} \text{ J}\cdot\text{s}$$

Max Kinetic Energy of a Photoelectron

$$KE_{\text{max}} = hf - hf_i$$

Wavelength of Matter Waves

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

Binding Energy & Mass Defect

$$\text{atomic mass of } H = 1.007825u$$

$$m_n = 1.008665u$$

$$c^2 = 931.49 \text{ MeV}/u$$

$$\Delta m = Z(\text{atomic mass of } H) + Nm_n - \text{atomic mass}$$

$$E_{\text{binding}} = \Delta mc^2$$

Activity (Decay Rate) & Half-Life

$$\text{Activity} = -\frac{\Delta N}{\Delta t} = \lambda N$$

$$T_{1/2} = \frac{0.693}{\lambda}$$